# The Main Parameters Effect OF Magnet Mass Analyzer And Electrostatic Quadruple Lens ON Beam Line System Design

#### Raheem Lafte Ali

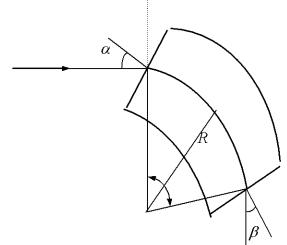
Al-Mustanseriyah, College of Education

#### **Abstract:**

In this research we consider a design at beam line system consisting of magnet mass analyzer and electrostatic quadruple lenses where changing the parameter (entrance angle  $\alpha$ , exit angle  $\beta$ , the distance between the lenses LD and quadruple lens length Lq). Also we study the action of the system focusing or defocusing by using the beam liner system.

#### Introduction

A charged particle beam is a group of particles that have about the same kinetic energy and move in about the same direction. A beam has a limited extent in the direction transverse to the average motion. The axis of charge particle beam can be represented by central trajectory and the axis may by curved if the beam passes through a transverse electric or magnetic field. Most applications of charged particle accelerations depend on the fact that beam particles have high energy. The beam transport system contains a magnet analyzer and electrostatic quadruple lens. Magnet represented the classic type of mass analyzer, and many designs have been perform and still are in use for magnetic sector instruments. The bent of the charged particles by the magnetic field leads to cleaning the beam from natural particles, then, focusing charged particles [1]. In design and manufacture of deflecting magnet, there are some parameter that must be regarded. Firstly, the entrance and exit edges  $(\alpha,\beta)$ , which are act as focusing regions that are resulted by a non-homogenous magnetic field .These regions are called a fringing field, as shown in figure (1). Secondly, the magnets field distributions vacuum gap which is inside magnet mass analyzer[2].



**Figure(1):** Magnet with nonzero entrance ( $\phi$ ) and exit ( $\beta$ ) angles [2].

The triplet consists of three singlet lenses of alternating polarity, are almost invariable symmetrical. That means the two outer elements are equal in length, strength and equally separated from the central element. So it may be derived from a doublet by dividing one of the elements into parts and placing the other element between them. The type of triplet depends on the arrangement of the singlet or doublet lenses forming it [3] as shown in figure (2).

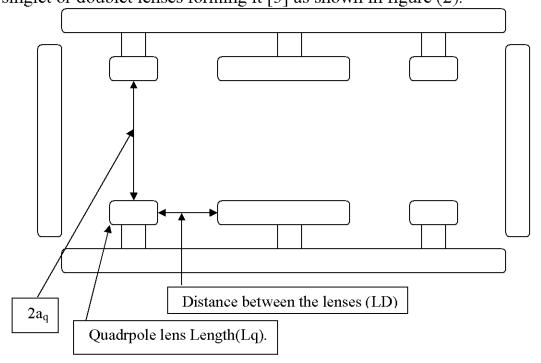


Figure (2): Triplet quadruple lens [2].

#### Mathematical treatment:

We represent a bundle of ray by a linear phase space matrix,  $\sigma$ -matrix, and for each region the relation between  $\sigma$ -matrix in two locations of the beam line is:

$$\sigma(out) = R \ \sigma(in) R^{T} \tag{1}$$

Where R: the 4×4 linear matrix, in the case of mid plane symmetry which leads no coupling in (x)and (y) plane.

After analyzing the motion of ion passing through the magnet and electrostatic quadruple lenses the total  $R_{\nu}$ -matrix of the magnet region is as follows:

$$R_x = R_x$$
 (exit edge).  $R_x$  (inside the magnet).  $R_x$  (entrance edge)

So that.

$$R_{x} = \begin{bmatrix} 1 & 0 \\ \frac{\tan \beta}{R} & 1 \end{bmatrix} \begin{bmatrix} \cos k_{x}l & \frac{1}{k_{x}} \sin k_{x}l \\ -k_{x} \sin k_{x}l & \cos k_{x}l \end{bmatrix} \begin{bmatrix} 1 & 0 \\ \frac{\tan \alpha}{R} & 1 \end{bmatrix}$$
(2)

While total  $R_y$ -matrix of the magnet region is:

 $R_y = R_y$  (exit edge).  $R_y$  (inside the magnet).  $R_y$  (entrance edge)

$$R_{y} = \begin{bmatrix} 1 & 0 \\ -\frac{\tan(\beta - \psi)}{R} & 1 \end{bmatrix} \begin{bmatrix} \cos k_{y}l & \frac{1}{k_{y}}\sin k_{y}l \\ -k_{y}\sin k_{y}l & \cos k_{y}l \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -\frac{\tan(\alpha - \psi)}{R} & 1 \end{bmatrix}$$
(3)

Where (R) is the radius of the central trajectory inside the magnet. (l) is the ion

beam path inside the magnet,  $(R_x = \frac{(1-n)^{\frac{1}{2}}}{R})$ ,  $(k_y = \frac{\sqrt{n}}{R})$ , (n) is the field index,

and  $(\psi)$  is the fringing field effect angle[4].

Sigma matrix for the quadruple triplet lens in *x*-plane:

### The Main Parameters Effect OF Magnet Mass Analyzer And Electrostatic Quadruple Lens ON Beam Line System Design .............. Raheem Lafte Ali

$$\sigma x_{11} (out) = \sigma x_{11} (in) + 4\sigma x_{12} (in) \left(2L_q + s\right) \left(1 + \theta^2 \left(1 + \frac{s}{L_q}\right)\right) \\
+ 4\sigma x_{22} (in) \left(2L_q + s\right)^2 \left(1 + \theta^2 \left(1 + \frac{s}{L_q}\right)\right)^2 \\
\sigma x_{12} (out) = -2\sigma x_{11} (in) \left(\frac{\theta^4}{L_q}\right) \left(\frac{2}{3} + \frac{s}{L_q}\right) + \sigma x_{12} (in) \left(1 - 4\frac{\theta^4}{L_q}\left(\frac{2}{3} + \frac{s}{L_q}\right)\left(2L_q + s\right)\right) \\
\left(1 + \theta^2 \left(1 + \frac{s}{L_q}\right)\right) + 2\sigma x_{22} (in) \left(2L_q + s\right) \left(1 + \theta^2 \left(1 + \frac{s}{L_q}\right)\right) \\
\sigma x_{21} (out) = \sigma x_{12} (in) \\
\sigma x_{22} (out) = 4\sigma x_{11} (in) \left(\frac{\theta^4}{L_q}\left(\frac{2}{3} + \frac{s}{L_q}\right)\right)^2 - 4\sigma x_{21} (in) \left(\frac{\theta^4}{L_q}\left(\frac{2}{3} + \frac{s}{L_q}\right) + \sigma x_{22} (in)\right) \tag{4}$$

In the same manner sigma matrix for the quadruple triplet lens in y-plane  $\sigma y_{21}(out)$  can be found.

Where Lq: is effective length of lens,  $\theta = wt = w\frac{L_q}{z}$  and (s) represents the relative length in (z) direction[5].

#### **Results and Discussion:**

In this study, we consider a design at beam line system consisting of magnet and quadruple setting the bending magnet first and the electrostatic quadruple lens second and changing the parameter of these devices. Also we study the action of the system focusing or defocusing by using the beam line system, these parameters change as:

- 1. Entrance angle  $\alpha$ =0°,10°
- 2. Exit angle  $\beta = 0^{\circ}, 10^{\circ}$
- 3. Distance lens(LD)=20mm,100mm
- 4. Quadruple lens length(Lq)=100mm,150mm

The schematic diagram of the system in this case represent as follows:

source First drift space(S1) Bending Second drift space (S2) Quadruple Third drift space (S2) Space(S3)
---

In case of horizontal plane, the entrance angle acts as divergence lens and exit angle acts as convergence lens as indicated in figures (1), (3) while in the vertical plane, the entrance angle acts as convergence lens and exit angle acts as divergence lens as indicated in figures (2), (4).

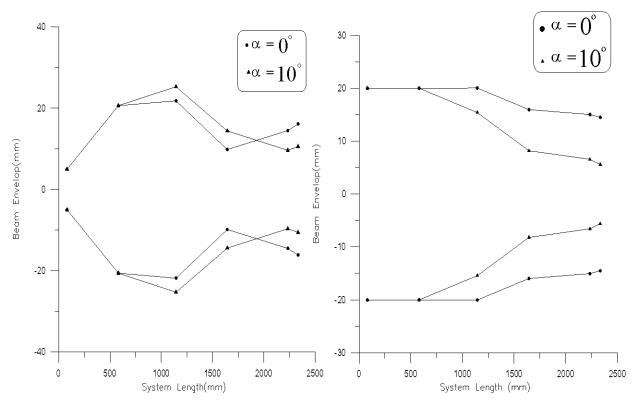
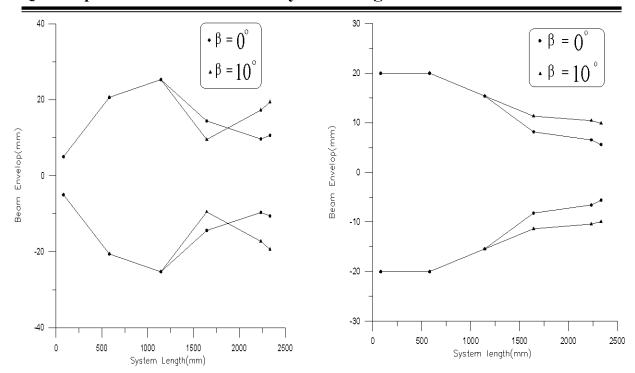


Figure (1): illustrates effect of entrance angle when exit angle=10,LD=20 and *Lq*=100mm in horizontal plane.

Figure(2):illustrates effect of entranceangle when exit angle=10,LD=20 and *Lq*=100mm in vertical plane.



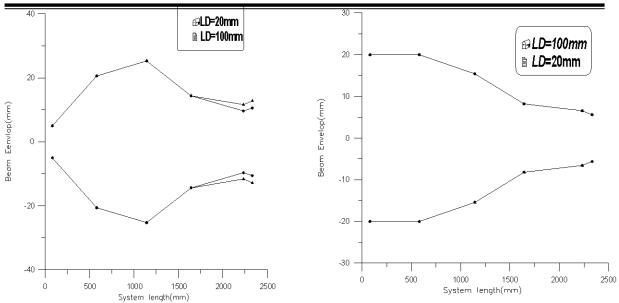
Figure(3):illustrates effect of exit anglewhen(entrance angle=10, LD=20mm and *Lq*=100mm in horizotal plane.

Figure (4): illustrates effect of exit anglewhen (entrance angle=10, LD=20mm and *Lq*=100mm in vertical plane.

For the increasing of distance between lenses LD it can be shown the defocusing (diverge) action of system in horizontal plane as shown in

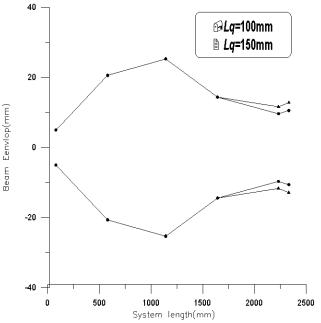
Figure (5) and there is no effect of LD on this action with constant beam envelope at the target as shown in figure (6) in the vertical plane because the initial angular divergence is small a value where initial angular divergence is the angle of the ray makes in the vertical plane with respect to the central trajectory.

In horizontal plane, the increasing of electrostatic quadruple lens length (Lq) causes defocusing action of the system as shown in figure (7). While In vertical plane, there is no action of quadruple lens length on focusing of quadruple lens but there is increasing in the system length with increasing quadruple lens length as indicate in figure (8) because there is increasing in the lenses length (Lq).

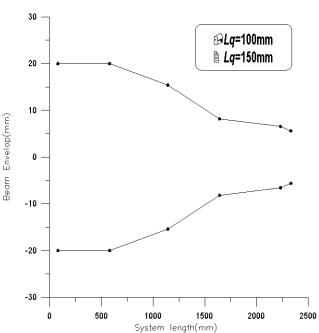


Figure(5):illustrates effect of distance between the lense when  $\alpha=10,\beta=10$  and Lq=100mm for horizontal plane.

Figure(6):illustrates effect of distance between the lenses when  $\alpha=10,\beta=10$  and Lq=100mm for vertical plane.



Figure(7):illustrates effect of quadrupole lens length when  $\alpha$ =10, $\beta$ =10 and lq=100mm for horizontal plane.



Figure(8):illustrates effect of quadrupole lens length when  $\alpha$ =10, $\beta$ =10 and  $\alpha$ =100mm for vertical plane.

#### Conclusions:

Form above results one can conclude that:

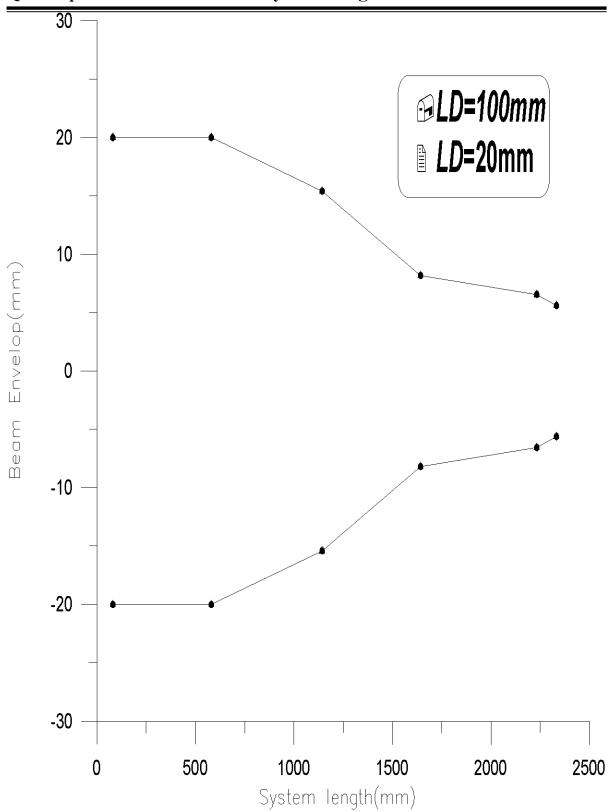
The bending magnet and electrostatic quadruple are important elements in the beam line system.

- The increasing entrance of entrance angle causes decreasing of the beam convergence in horizontal plane and increasing of the beam convergence in vertical plane so that the entrance angle acts as a divergence thin lens in horizontal plane and as a convergence thin lens in vertical plane.
- The exit angle acts as a convergence thin lens in horizontal plane and as a divergence thin lens in vertical plane.
- The increasing of distance between the lenses (LD) and the quadruple lens length (Lq) cause decreasing of beam convergence in horizontal plane and there is no change in beam focusing in vertical plane.
- The best design for this research is:  $(\alpha=0^{\circ},\beta=10^{\circ}, LD=20 \text{mm} \text{ and } Lq=100 \text{mm})$

#### References:

- 1. A.P. Banford" The Transport of Charged-Particle Beams", E. and F.N.SPON Limited, London, 1966.
- 2. H.F.Glavish, "Magnet Optics for Beam Transport", Nucl.Instr. and Meth., 189(1981).
- 3. S.Humphries, Jr." principles of Charged Particle Acceleration" University of New Mexico, 1999.
- 4. I.H.Hashim." A Study Of The Main Parameters Effect In Designing The Medium Range Ion Implanter "PhD thesis, Al-Mustanseriyah University, 2004.
- 5. Alsadiq AL.NAEEM" Waist to Waist Transport Of Charged Particles Beam In Different Optical Elements" MSC thesis, Al-Mustanseriyah University, 2010.

The Main Parameters Effect OF Magnet Mass Analyzer And Electrostatic Quadruple Lens ON Beam Line System Design .............. Raheem Lafte Ali



The Main Parameters Effect OF Magnet Mass Analyzer And Electrostatic Quadruple Lens ON Beam Line System Design .............. Raheem Lafte Ali

## تأثير العوامل الرئيسية لمغناطيس التحلل الكتلى والعدسات الالكتروستاتيكية الرباعية على تصميم منظومة نقل الحزمة

\*رحيم لفتة علي\* \*الجامعة المستنصرية- كلية التربية\*

#### الخلاصة:

البحث الحالي يتضمن تصميم نظام مسار حزمة يتكون من مغناطيس التحليل الكتلي والعدسات الكهروستاتيكية رباعية القطب وبتغير كل من (زاوية الدخول $\alpha$ ، زاوية الخروج  $\beta$ ، المسافة بين العدسات LD وطول العدسة الرباعية ( $L_{\alpha}$ ) وكذلك دراستها كأنظمة تبئير وتشتت.